

# A Strongly Asymptotically Optimal Agent in General Environments

Michael K. Cohen, Elliot Catt, Marcus Hutter



Australian National University

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## Central result

- \* Our agent's policy's value approaches the optimal value in *any computable* environment.
- \* No finite-state Markov or ergodicity assumption is required.

# Exploitation vs. exploration

When should you:

- \* Go to your favorite restaurant
- \* Fund space travel using current materials
- \* Sell trinkets where you've had the best luck
- \* Try a new restaurant
- \* Fund materials science
- \* Revisit another place

*"Efforts to solve [an instance of the exploration-exploitation problem] so sapped the energies and minds of Allied analysts that the suggestion was made that the problem be dropped over Germany, as the ultimate instrument of intellectual sabotage." –Peter Whittle*

# Motivation: exploring when novel states abound

**Claim:** environments that enter completely novel states infinitely often render (PO)MDP-inspired exploration strategies helpless.

## Example environments hard to model as an MDP:

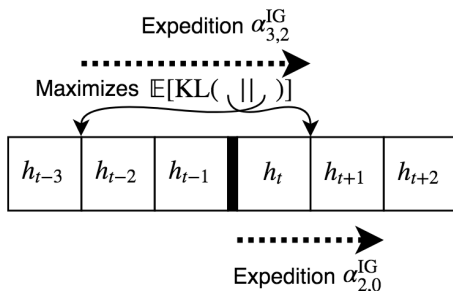
- \* chatbot
- \* function optimizer
- \* theorem prover

# Bayesian Reinforcement Learning

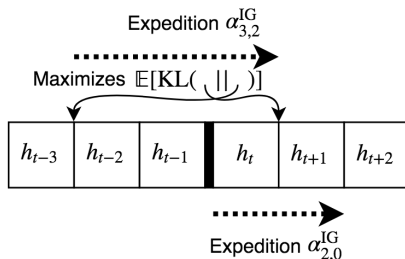
- \* Start with a prior distribution over what the environment is
- \* Update this into a posterior distribution
- \* Maximize expected reward using current “beliefs”

# Exploratory Expeditions

- \* Explore to maximize **information gain**
- \*  $m$ -step information gain = how poorly current posterior over environments approximates posterior after  $m$  steps (using KL-divergence)
- \*  $m$ - $k$  expedition is the  $m$ -step-info-gain-maximizing policy that began  $k$  steps ago



# Inquisitive Reinforcement Learner (Inq)



- \* Follow the  $m$ - $k$  exploratory expedition ( $\alpha_{m,k}^{\text{IG}}$ ) with probability proportional to expected info-gain (but capped at  $\frac{1}{m^2(m+1)}$ ).
- \* Else: exploit as a Bayesian reinforcement learner.

# Strong asymptotic optimality

**Value of policy**  $\pi$  in environment  $\nu$  after interaction history  $h_{<t}$ :

$$V_{\nu}^{\pi}(h_{<t}) := \frac{1}{\sum_{k=t}^{\infty} \gamma_k} \mathbb{E}_{\nu}^{\pi} \left[ \sum_{k=t}^{\infty} \gamma_k r_k \mid h_{<t} \right]$$

**Strong asymptotic optimality:** for all computable environments  $\mu$ ,

$$V_{\mu}^{*}(h_{<t}) - V_{\mu}^{\pi}(h_{<t}) \xrightarrow{t \rightarrow \infty} 0 \text{ with } P_{\mu}^{\pi}\text{-prob. } 1$$

## Main Result:

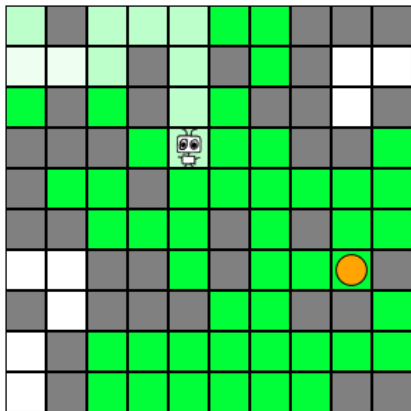
For an agent with a bounded horizon<sup>a</sup>, Inq's policy  $\pi$  is strongly asymptotically optimal.

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<sup>a</sup>bounded horizon = not becoming more farsighted over time; formally,  
 $\forall \varepsilon \exists m \forall t : (\sum_{k=t+m}^{\infty} \gamma_k) / (\sum_{k=t}^{\infty} \gamma_k) \leq \varepsilon$

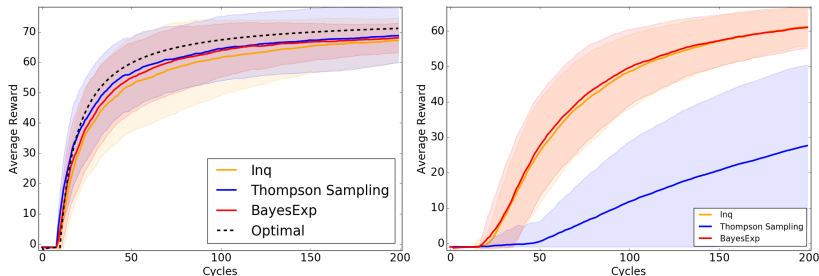


# Experiments



*Gridworld environment. Reward dispensed with probability  $3/4$  at ●. Model class is that the reward dispenser could be at any accessible square. Green is agent's posterior probability reward dispenser is there.*

# Experimental results



*Average reward accumulated in 10x10 (left) and 20x20 (right) gridworlds. Inq is compared to weakly asymptotically optimal agents.*

We approximate Inq tractably by replacing expectimax with  $\rho$ UCT, and restricting the planning horizon.

Thank you